

### COMMONLY USED FORMULAS IN STRUCTURAL ANALYSIS

CALCULATING ACTUAL STRESS:

$$\text{bending: } f_b = \frac{M}{S}$$

$$\text{axial: } f_a = \frac{P}{A}$$

$$\text{shear: } f_v = \frac{3}{2} \frac{V}{A} \quad (\text{rectangular cross section only})$$

SECTION PROPERTIES FOR A RECTANGULAR CROSS SECTION:

$$I = \frac{bd^3}{12} \quad S = \frac{I}{c} = \frac{bd^2}{6} \quad A = bd$$

MIDSPAN DEFLECTION OF A SIMPLY-SUPPORTED, UNIFORMLY LOADED BEAM:

$$\Delta = \frac{5wL^4}{384EI} \quad \text{note: } w \text{ denotes the distributed load (e.g. kips per foot)}$$

BUCKLING THEORY:

$$P_{cr} = \frac{\pi^2 EI}{(kL)^2}$$

$$f_{cr} = \frac{P_{cr}}{A} = \frac{\pi^2 EI}{(kL)^2 A} = \frac{\pi^2 E}{\left(\frac{kL}{r}\right)^2}$$

$$r = \sqrt{\frac{I}{A}}$$

DESIGN CRITERIA: (actual stress)  $\leq$  (allowable stress)

- Bending stress:  $f_b \leq F_b$
- Shear stress:  $f_v \leq F_v$
- Axial stress:  $f_a \leq F_a$   
where  $F_a$  is the allowable stress in tension or compression.

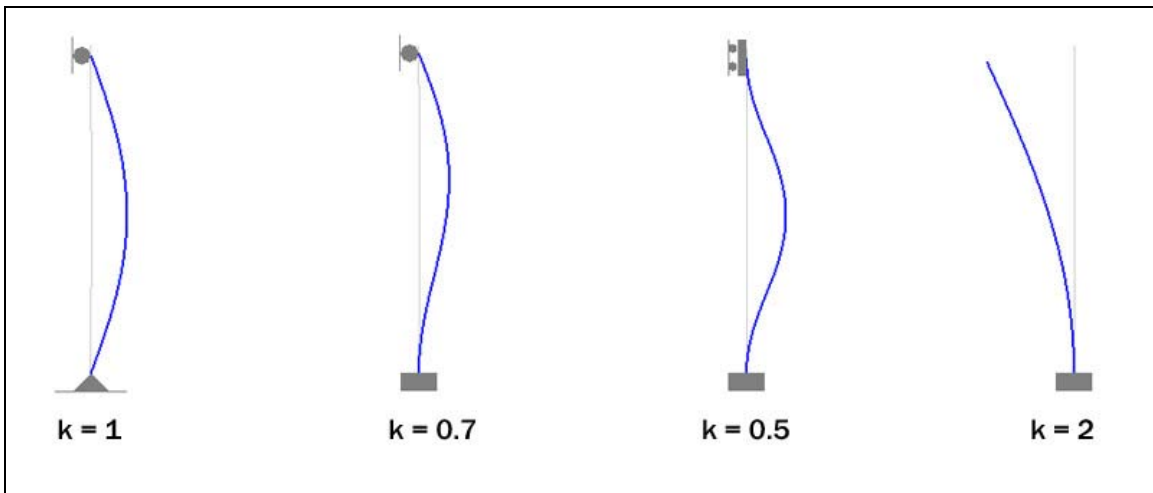
The allowable compression stress is the smallest of:

allowable crushing stress	$F_c$
allowable weak-axis buckling stress	$F_{cr_y}$
allowable strong-axis buckling stress	$F_{cr_x}$

where the allowable buckling stress is:

$$F_{cr} = \frac{f_{cr}}{\text{Factor of Safety}}$$

- Effective length factors for various column end conditions:



- Interaction formula for combined bending and axial stress:

$$\frac{f_a}{F_a} + \frac{f_b}{F_b} \leq 1$$